To Rose Mary —E.A.

To Vicki, Bonnie, Bob, Cookie, and Goatee —D.S.
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This book is an introduction to computer graphics with an emphasis on applications programming. The first edition, which was published in 1997, was somewhat revolutionary in using OpenGL and a top-down approach. Over the succeeding 22 years and seven editions, this approach has been adopted by most introductory classes in computer graphics and by virtually all the competing textbooks.

A Top-Down Approach

Recent advances and the success of the first seven editions continue to reinforce our belief in a top-down, programming-oriented approach to introductory computer graphics. Although many computer science and engineering departments now support more than one course in computer graphics, most students will take only a single course. Such a course usually is placed in the curriculum after students have already studied programming, data structures, algorithms, software engineering, and basic mathematics. Consequently, a class in computer graphics allows the instructor to build on these topics in a way that can be both informative and fun. We want these students to be programming three-dimensional applications as soon as possible. Low-level algorithms, such as those that draw lines or fill polygons, can be dealt with later, after students are creating graphics.

When asked “why teach programming?”, John Kemeny, a pioneer in computer education, used a familiar automobile analogy: You don’t have to know what’s under the hood to be literate, but unless you know how to program, you’ll be sitting in the back seat instead of driving. That same analogy applies to the way we teach computer graphics. One approach—the algorithmic approach—is to teach everything about what makes a car function: the engine, the transmission, the combustion process. A second approach—the survey approach—is to hire a chauffeur, sit back, and see the world as a spectator. The third approach—the programming approach that we have adopted here—is to teach you how to drive and how to take yourself wherever you want to go. As an old auto rental commercial used to say, “Let us put you in the driver’s seat.”

The sixth and seventh editions reflected the major changes in graphics application development due to advances in graphics hardware. In particular, the sixth edition was fully shader-based, enabling readers to create applications that could fully exploit the capabilities of modern GPUs. We noted that these changes were part of OpenGL ES 2.0, which was being used to develop applications for embedded systems and handheld devices, such as cell phones and tablets, and of WebGL, its JavaScript implementation. At the time, we did not anticipate the extraordinary
interest in WebGL that began as soon as web browsers became available that sup-
port WebGL through HTML5. For the seventh edition, we switched from desktop
OpenGL to WebGL.

As we noted then, WebGL applications were running everywhere, including on
some of the latest smart phones, and even though WebGL lacks some of the advanced
features of the latest versions of OpenGL, the ability to integrate it with HTML5
opened up a wealth of new application areas. As an added benefit, we found it much
better suited than desktop OpenGL for teaching computer graphics. Our hopes for
the seventh edition were more than fulfilled. WebGL has proven to be excellent API
for both teaching and developing real applications that run on all platforms.

In particular, features of the seventh edition included:

- WebGL 1.0 was used for all examples and programs.
- All code was written in JavaScript.
- All code runs in recent web browsers.
- A new chapter on interaction was added.
- Additional material on render-to-texture was added.
- Additional material on displaying meshes also was added.
- An efficient matrix–vector package was included.
- An introduction to agent-based modeling was added.

For the eighth edition, building on the success of using WebGL, we have:

- Updated all examples and programs to WebGL 2.0.
- Added many additional examples.
- Switched to a fully electronic version that includes links to examples so they
can be viewed with the code while reading.
- Expanded coverage of render-to-texture in a separate chapter that includes
new topics, including shadow maps and projective textures.
- Added coverage of three-dimensional texture mapping.
- Updated the chapter on modeling to include an introduction to three.js, a
popular higher-level JavaScript scene-graph API.
- Added coverage of point sprites for simulation.
- Expanded and updated our coverage of rendering.
- Enhanced discussions of hardware implementation and GPU architectures.

Programming with WebGL and JavaScript

When Ed began teaching computer graphics 35 years ago, the greatest impediment
to implementing a programming-oriented course, and to writing a textbook for that
course, was the lack of a widely accepted graphics library or application programming
interface (API). Difficulties included high cost, limited availability, lack of generality,
and high complexity. The development of OpenGL resolved most of the difficulties
many of us had experienced with other APIs and with the alternative of using home-brewed software. OpenGL today is supported on all platforms and is widely accepted as the cross-platform standard. WebGL builds on OpenGL’s wide acceptance (it’s effectively the same API), but provides a more accessible development platform using web technologies.

A graphics class teaches far more than the use of a particular API, but a good API makes it easier to teach key graphics topics, including three-dimensional transformations, lighting and shading, client–server graphics, modeling, and implementation algorithms. We believe that OpenGL’s extensive capabilities and well-defined architecture lead to a stronger foundation for teaching both theoretical and practical aspects of the field and for teaching advanced concepts, including texture mapping, compositing, and programmable shaders.

Ed switched his classes to OpenGL about 24 years ago and the results astounded him. By the middle of the semester, every student was able to write a moderately complex three-dimensional application that required understanding of three-dimensional viewing and event-driven input. In the previous years of teaching computer graphics, he had never come even close to this result. That class led to the first edition of this book.

This book is a textbook on computer graphics; it is not an OpenGL or WebGL manual. Consequently, it does not cover all aspects of the WebGL API but rather explains only what is necessary for mastering this book’s contents. It presents WebGL at a level that should permit users of other APIs to have little difficulty with the material.

Unlike earlier editions, this one uses WebGL and JavaScript for all the examples. WebGL 2.0 is a JavaScript implementation of OpenGL ES 3.0 and runs in most recent browsers. Because it is supported by HTML5, not only does it provide compatibility with other applications but also there are no platform dependences; WebGL runs within the browser and makes use of the local graphics hardware. Although JavaScript is not the usual programming language with which we teach most programming courses, it is the language of the Web. Over the past few years, JavaScript has become increasingly more powerful, and our experience is that students who are comfortable with Java, Python, C, or C++ will have little trouble programming in JavaScript. So that we can continue to support a wide audience with varied backgrounds, we have kept with a very basic JavaScript requiring only ES5. Students who have more experience with JavaScript should have little trouble updating our examples and libraries to exploit powerful new JavaScript features contained in ES6.

All the modern versions of OpenGL, including WebGL, require every application to provide two shaders written in the OpenGL Shading Language (GLSL). GLSL is similar to C but adds vectors and matrices as basic types, along with some C++ features, such as operator overloading. We provide a JavaScript library, MVJjs, that supports both our presentation of graphics functions and the types and operations in GLSL. It also contains many functions that perform operations equivalent to deprecated functions from the earlier fixed-function versions of OpenGL.
Intended Audience

This book is suitable for advanced undergraduates and first-year graduate students in computer science and engineering and for students in other disciplines who have good programming skills. The book also will be useful to many professionals. Between us, we have taught well over 100 short courses for professionals (including many courses presented at the annual SIGGRAPH conferences, two of which are available on YouTube within the SIGGRAPH University channel), and even a Massive Online Course (MOOC) with Coursera. Our experiences with these nontraditional students have had a great influence on what we chose to include in the book.

Prerequisites for the book are good programming skills in JavaScript, Python, C, C++, or Java; an understanding of basic data structures (arrays, linked lists, trees); and a rudimentary knowledge of linear algebra and trigonometry. We have found that the mathematical backgrounds of computer science students, whether undergraduates or graduates, vary considerably. Hence, we have chosen to integrate into the text much of the linear algebra and geometry that is required for fundamental computer graphics.

Organization of the Book

The book is organized as follows:

- Chapter 1 provides an overview of the field and introduces image formation by optical devices; thus, we start with three-dimensional concepts immediately.
- Chapter 2 introduces programming using WebGL. Although the first example program that we develop (each chapter has one or more complete programming examples) is two-dimensional, it is embedded in a three-dimensional setting and leads to a three-dimensional extension.
- Chapter 3 introduces interactive graphics and develops event-driven graphics within the browser environment.
- Chapters 4 and 5 concentrate on three-dimensional concepts. Chapter 4 is concerned with defining and manipulating three-dimensional objects, whereas Chapter 5 is concerned with viewing them.
- Chapter 6 introduces light–material interactions and shading.
- Chapters 7 and 8 introduce many of the new discrete capabilities that are now supported in graphics hardware and by WebGL. All these techniques involve working with various buffers. Chapter 7 focuses on classical texture mapping with a single texture, whereas Chapter 8 concentrates on texture mapping using off-screen buffers.

These chapters should be covered in order and can be taught in about 10 weeks of a 15-week semester.

The last five chapters can be read in almost any order. All five are somewhat open-ended and can be covered at a survey level, or individual topics can be pursued in depth.
Chapter 9 includes a number of topics that fit loosely under the heading of hierarchical modeling. The topics range from building models that encapsulate the relationships between the parts of a model, to high-level approaches to graphics over the Internet. Chapter 9 also includes an introduction to scene graphs.

Chapter 10 introduces a number of procedural methods, including particle systems, fractals, and procedural noise.

Chapter 11 discussed curves and surfaces, including subdivision surfaces.

Chapter 12 surveys implementations. It gives one or two major algorithms for each of the basic steps, including clipping, line generation, and polygon fill.

Finally, Chapter 13 surveys alternate approaches to rendering. It includes expanded discussions of ray tracing and radiosity, and an introduction to image-based rendering, parallel rendering, and concepts of virtual and augmented reality.

Several appendices are included to provide additional reference:

- Appendix A presents the details of the WebGL functions needed to read, compile, and link the application and shaders.
- Appendices B and C contain a review of the background mathematics.
- Appendix D discusses sampling and aliasing starting with Nyquist’s theorem and applying these results to computer graphics.

Changes from the Seventh Edition

The reaction of readers to the first seven editions of this book was overwhelmingly positive, especially to the use of OpenGL/WebGL and the top-down approach. In the sixth edition, we abandoned the fixed-function pipeline and went to full shader-based OpenGL. In the seventh edition, we moved to WebGL, which is not only fully shader based—each application must provide a vertex shader and a fragment shader—but also a version that works within the latest web browsers.

Moving to an only online format for this edition allowed us make some interesting, and, we think, positive changes. First, all the figures are now in full color. We have moved the images from the color insert into regular figures in the chapters, which places them where they should be. We were also able to add screen shots from our examples as regular figures. The URLs for these examples are in the figure captions. Thus, students will be able to use the URL to open another browser window to run the example. Most browsers will also let the student examine the full code in another window. We believe these features will greatly enhance the examples. We have also added many new examples to the book’s website (www.interactivecomputergraphics.com/Code), which are accessible through links at the end of each chapter.

For this edition, we updated all our code to use WebGL 2.0. Although we introduce few additional WebGL 2.0 features—three-dimensional texture mapping being
an exception—the newer version of GLSL results in much clearer shader code. For examples that do not use new features, we will keep WebGL 1.0 versions on the book’s website.

Applications are written in JavaScript. Although JavaScript has its own idiosyncrasies and may not be the language used in students’ programming courses, we have not observed any problems with students using JavaScript. JavaScript has many variants, which students and instructors may prefer to use. In addition, there are many ways to develop code in other languages and use a transpiler to produce JavaScript. Because many of these options are new and perhaps transient, we have stuck with a very basic JavaScript that should run everywhere.

We have added additional material on off-screen rendering and render-to-texture, including techniques such as projective textures and shadow maps. We have also added material on using GPUs for a variety of compute-intensive applications, such as image processing and simulation. We have also added coverage of three-dimensional texture, an added feature in WebGL 2.0, and its use for volume visualization. Because of the large amount of added material, we split the former Chapter 7 into two chapters: 7 and 8.

Given the positive feedback we have received on the core material from Chapters 1–6 in previous editions, other than updating the code to WebGL 2.0, we have tried to keep the changes to those chapters to a minimum. We see Chapters 1–8 as the core of any introductory course in computer graphics. Chapters 9–13 can be used in almost any order, either as a survey in a one-semester course or as the basis of a two-semester sequence.

Chapter 9 has been updated to be more consistent with three.js scene graphs, and includes a short introduction to the three.js API. Chapter 11 adds material on using point sprites in particle simulations.

Chapter 11 is largely unchanged. Material on implementation that was formerly in Chapter 8 in the seventh edition has been moved to Chapter 12. As interesting as we find many of the classic algorithms for tasks such as line generation and clipping, this material is no longer a core part of most first courses on Computer Graphics. We have kept the parts of the chapter that are still highly relevant and taken out parts that are no longer used in modern GPUs. Chapter 13 (formerly Chapter 12) has been updated to cover some additional approaches to rendering such as deferred shading.

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Ed Angel
Dave Shreiner